## Mathematics

Sample Graduation Proficiencies \& Performance Indicators

VT CONTENT AReA Graduation Proficiencies \& Performance Indicators:

- Are required by Section 2120.8 of the education quality standards
- Reflect existing learning standards required by the Vt State Board of Education, under the VT Framework of Standards (CCSS, NGSS, AND GES)
- Are designed to be used in conjunction with the VT Transferable Skills Graduation PROFICIENCIES, WHICH OUTLINE STUDENTS' DESIRED SKILLS AND HABITS ACROSS CONTENT AREAS
- INCLUDE THREE SETS OF PERFORMANCE INDICATORS DIFFERENTIATED BY GRADE CLUSTER— ELEMENTARY, MIDDLE, AND HIGH SCHOOL
- SERVE AS BENCHMARKS OF LEARNING PROGRESSION FOR ELEMENTARY AND MIDDLE SCHOOL

THIS DOCUMENT IS DESIGNED TO:

- Assist Vermont schools and Districts/SUs in developing learning requirements and EXPECTATIONS FOR THEIR STUDENTS
- Promote consistency across schools and Districts/SUs for Transfer Students
- InCREASE PERSONALIZATION AND FLEXIBILITY FOR INSTRUCTION AND LEARNING
- Help build curriculum and steer assessment development
- SUPPORT FORMATIVE ASSESSMENT PRACTICES, INCLUDING PERFORMANCE ASSESSMENT
- SIMULTANEOUSLY PROVIDE DATA AND INSIGHT INTO ACHIEVEMENT WHEN ALIGNED WITH THE TRANSFERABLE SKILLS
- SUPPORT STUDENT ACHIEVEMENT OF THE EXPECTED CONTENT STANDARDS

| GRADUATION PROFICIENCIES | PERFORMANCE INDICATORS—ELEMENTARY SCHOOL | PERFORMANCE INDICATORS-MIDDLE SCHOOL | PERFORMANCE INDICATORS-HIGH SCHOOL |
| :---: | :---: | :---: | :---: |
| 1. MODELING <br> Use mathematics to help make sense of the real world: identify variables, formulate a model describing the relationship between the variables, interpret results, and validate and report conclusions and the reasoning behind them. | a. Use numerical phenomena or quantities to model a situation. <br> b. Use geometric shapes and their properties to model physical objects. <br> c. Use equations to model and interpret situations. <br> d. Use graphing techniques to model situations involving data. <br> e. Compare mathematical models for a situation. <br> f. Interpret the results of applying the model in the context of the situation. | a. Use numerical phenomena or quantities to model a situation. <br> b. Use geometric shapes and their properties to model physical objects. <br> c. Use equations, inequalities and functions to model and interpret situations. <br> d. Use statistics to model situations involving data. <br> e. Compare mathematical models for a situation. <br> f. Interpret the results of applying the model in the context of the situation. | a. Use numerical phenomena or quantities to a model a situation. (HSN.Q) <br> b. Use geometric shapes and their properties to model physical objects. (HSG.SRT.C, GPE.B, GMD.A, MG) <br> c. Use equations, inequalities and functions to model and interpret situations. (HSA.SSE, CED, REI.D; HSF.IF.B,C, BF.A, LE, TF.B) <br> d. Use statistics to model situations involving data. (HSS) <br> e. Compare mathematical models for a situation. <br> f. Interpret the results of applying the model in the context of the situation. |


| GRADUATION PROFICIENCIES | PERFORMANCE INDICATORS-ELEMENTARY SCHOOL | PERFORMANCE INDICATORS-MIDDLE SCHOOL | PERFORMANCE INDICATORS-HIGH SCHOOL |
| :---: | :---: | :---: | :---: |
| 2. NUMBER AND QUANTITY <br> Reason, describe, and analyze quantitatively, using units and number systems to solve problems. | a. Understand the place value system. (5NBT.A) <br> b. Perform operations with multi-digit whole numbers and with decimals to hundredths. (5NBT.B) <br> c. Use equivalent fractions as a strategy to add and subtract fractions. (5NF.A) <br> d. Apply and extend previous understandings of multiplication and division to multiply and divide fractions. (5NF.B) | a. Compute fluently with multi-digit numbers and find common factors and multiples. (6NS.A) <br> b. Apply and extend previous understandings of numbers to the system of rational numbers. (6NS.B) <br> c. Apply and extend previous understandings of operations with fractions. (7NS.A) <br> d. Know that there are numbers that are not rational, and approximate them by rational numbers. (8NS.A) | a. Extend the properties of exponents to rational exponents. (HSN.RN.A) <br> b. Use the properties of rational and irrational numbers. (HSN.RN.B) <br> c. Reason quantitatively and use units to solve problems. (HSN.Q.A) <br> d. Perform arithmetic operations with complex numbers. (HSN.CN.A) <br> e. Use complex numbers in polynomial identities and equations. (HSN.CN.C) |
| 3. ALGEBRA <br> Create, interpret, use, and analyze expressions, equations and inequalities. | a. Write and interpret numerical expressions. (50A.A) | a. Apply and extend previous understandings of arithmetic to algebraic expressions. (6EE.A) <br> b. Reason about and solve one-variable equations and inequalities. (6EE.B) <br> c. Represent and analyze quantitative relationships between dependent and independent variables. (6EE.C) <br> d. Use properties of operations to generate equivalent expressions. (7EE.A) <br> e. Solve real-life and mathematical problems using numerical and algebraic expressions and equations. (7EE.B) <br> f. Work with radicals and integer exponents. (8EE.A) <br> g. Understand the connections between proportional relationships, lines, and linear equations. (8EE.B) <br> h. Analyze and solve linear equations and pairs of simultaneous linear equations. (8EE.C) | a. Interpret the structure of expressions.(HSA.SSE.A) <br> b. Write expressions in equivalent forms to solve problems. (HSA.SSE.B) <br> c. Perform arithmetic operations on polynomials. (HSA.APR.A) <br> d. Understand the relationship between zeros and factors of polynomials. (HSA.APR.B) <br> e. Use polynomial identities to solve problems. (HSA.APR.C) <br> f. Rewrite rational expressions. (HSA.APR.D) <br> g. Create equations that describe numbers or relationships. (HSA.CED.A) <br> h. Understand solving equations as a process of reasoning and explain the reasoning. (HSA.REI.A) <br> i. Solve equations and inequalities in one variable. (HSA.REI.B) <br> j. Solve systems of equations. (HSA.REI.C) <br> k. Represent and solve equations and inequalities graphically. (HSA.REI.D) |


| GRADUATION PROFICIENCIES | PERFORMANCE INDICATORS—ELEMENTARY SCHOOL | PERFORMANCE INDICATORS-MIDDLE SCHOOL | PERFORMANCE INDICATORS-HIGH SCHOOL |
| :---: | :---: | :---: | :---: |
| 4. FUNCTIONS <br> Use functions, including linear, quadratic, trigonometric and exponential, to interpret and analyze a variety of contexts. | a. Analyze patterns and relationships. (50A.B) | a. Understand ratio concepts and use ratio reasoning to solve problems. (6RP.A) <br> b. Analyze proportional relationships and use them to solve real-world and mathematical problems. (7RP.A) <br> c. Define, evaluate, and compare functions. (8F.A) <br> d. Use functions to model relationships between quantities. (8F.B) | a. Understand the concept of a function and use function notation. (HSF.IF.A) <br> b. Interpret functions that arise in applications in terms of the context. (HSF.IF.B) <br> c. Analyze functions using different representations. (HSF.IF.C,E) <br> d. Build a function that models a relationship between two quantities. (HSF.BF.A) <br> e. Build new functions from existing functions. (HSF.BF.B) <br> f. Construct and compare linear, quadratic, and exponential models and solve problems. (HSF.LE.A) <br> g. Interpret expressions for functions in terms of the situation they model. (HSF.LE.B) <br> h. Extend the domain of trigonometric functions using the unit circle. (HSF.TF.A) <br> i. Model periodic phenomena with trigonometric functions. (HSF.TF.B) <br> j. Prove and apply trigonometric identities. (HSF.TF.C) |
| 5. GEOMETRY <br> Understand geometric concepts and constructions, prove theorems, and apply appropriate results to solve problems. | a. Graph points on the coordinate plane to solve realworld and mathematical problems. (5G.A) <br> b. Classify two-dimensional figures into categories based on their properties. (5G.B) | a. Solve real-world and mathematical problems involving area, surface area, and volume. (6G.A) <br> b. Draw construct, and describe geometrical figures and describe the relationships between them. (7G.A) <br> c. Solve real-life and mathematical problems involving angle measure, area, surface area, and volume. (7G.B) <br> d. Understand congruence and similarity using physical models, transparencies, or geometry software. (8G.A) <br> e. Understand and apply the Pythagorean Theorem. (8G.B) | a. Experiment with transformations in the plane. (HSG.CO.A) <br> b. Understand congruence in terms of rigid motions. (HSG.CO.B) <br> c. Prove geometric theorems. (HSG.CO.C) <br> d. Make geometric constructions. (HSG.CO.D) <br> e. Understand similarity in terms of similarity transformations. (HSG.SRT.A) <br> f. Prove theorems involving similarity. (HSG.SRT.B) <br> g. Define trigonometric ratios and solve problems involving right triangles. (HSG.SRT.C) |


| GRADUATION PROFICIENCIES | PERFORMANCE INDICATORS—ELEMENTARY SCHOOL | PERFORMANCE INDICATORS-MIDDLE SCHOOL | PERFORMANCE INDICATORS-HIGH SCHOOL |
| :---: | :---: | :---: | :---: |
|  |  | f. Solve real-world and mathematical problems involving volume of cylinders, cones, and spheres. (8G.C) | h. Understand and apply theorems about circles. (HSG.C.A) <br> i. Find arc lengths and areas of sectors of circles. (HSG.C.B) <br> j. Translate between the geometric description and the equation for a conic section. (HSG.GPE.A) <br> k. Use coordinates to prove simple geometric theorems algebraically. (HSG.GPE.B) <br> I. Explain volume formulas and use them to solve problems. (HSG.GMD.A) <br> m. Visualize relationships between two-dimensional and three-dimensional objects. (HSG.GMD.B) <br> n. Apply geometric concepts in modeling situations. (HSG.MG.A) |
| 6. STATISTICS \& PROBABILITY <br> Interpret and apply statistics and probability to analyze data, reach and justify conclusions, and make inferences. | a. Convert like measurement units within a given measurement system. (5MD.A) <br> b. Represent and interpret data. (5MD.B) <br> c. Geometric measurement: understand concepts of volume. (5MD.C) | a. Develop understanding of statistical variability. (6SP.A) <br> b. Summarize and describe distributions. (6SP.B) <br> c. Use random sampling to draw inferences about a population. (7SP.A) <br> d. Draw informal comparative inferences about two populations. (7SP.B) <br> e. Investigate chance processes and develop, use, and evaluate probability models. (7SP.C) <br> f. Investigate patterns of association in bivariate data. (8SP.A) | a. Summarize, represent, and interpret data on a single count or measurement variable. (HSS.ID.A) <br> b. Summarize, represent, and interpret data on two categorical and quantitative variables. (HSS.ID.B) <br> c. Interpret linear models. (HSS.ID.C.) <br> d. Understand and evaluate random processes underlying statistical experiments. (HSS.IC.A.) <br> e. Make inferences and justify conclusions from sample surveys, experiments, and observational studies. (HSS.IC.B.) <br> f. Understand independence and conditional probability and use them to interpret data. (HSS.CP.A.) <br> g. Use the rules of probability to compute probabilities of compound events in a uniform probability model. (HSS.CP.B.) |

